Design and Analysis of Three Phase Induction Motor using Computer Program

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ABSTRACT [ENGLISH/ANGLAIS]
In the recent years it has been noticed that the induction motor has become the workhorse of the industrial sector of any economy. This is as a result of its easy means of construction and maintenance. Since the motor is being used for different purposes in the industries, the need to have an easy way of designing the machine arises. The basic design of an electrical machine, that is the dimensioning of the magnetic and electric circuits, is usually carried out by applying analytical equations. However, accurate performance of the machine is usually evaluated using computer aided design method. With this Computer aided design (CAD) method, the effect of a single parameter on the dynamical performance of the machine can be effectively studied by using a computer programming language. This paper presents a CAD approach (using java) in carrying out the design calculations which made the design of three phase induction easy.

Keywords: CAD, java, design, parameters, accurate performance

INTRODUCTION
With the recent trend in Technology, most lengthy calculations and simulation of circuits are done with the use of computer programs designed to serve different purposes. Examples of such programs include Matlab, C++, java, etc.

Computer aided design (CAD) is the use of computer to assist in design processes. Specialised software packages exist for various types of design: architectural, engineering, electronics, highways and woven fabrics to mention but a few. It is generally possible to generate engineering drawings that gives detailed information on the final design to be constructed. CAD is also the modelling of physical systems on Computer, allowing both interactive and automatic analysis of design variants and the expression of design in a form suitable for manufacturing [1]. All CAD systems have potentials that could lead to many important benefits for organizations. For example, CAD systems can reduce the length of the product development cycle and improve relationships with both vendors and customers. Many literatures provide many descriptions of CAD applications that have helped to reduce the product development time [2, 3]. A shorter design cycle makes companies to respond more quickly to competitive challenges, incorporate newer technology into products, and charge higher prices for special features [4].

Three phase induction motor finds its application in almost all facets of life and thus its demand is high and it is thus advisable to design a program that aids in the
computation of the parameters required for the construction in order to save time and reduce the errors associated with the analytical method. In this work we basically are concerned with the computer aided design of three phase induction motor using Java programming language since the analytical process is time consuming and so laborious. The language used for the development of this software is Java. Java is a general purpose, concurrent, class-based, object-oriented language that is specifically designed to have as few implementation dependencies as possible [5]. It is intended to let application developers “Write once, Run anywhere” [6]. The reason for our choice of java as a programming language is because it is robust, secure and portable; it also allows the programmer to create controls and then write codes for each control so that it could be executed at the press of a command button [5]. The program shall be presented in a graphical user interface (GUI).

MATERIALS AND METHODS

Design Specifications
The main specifications for the design of a three phase induction motor are: rated output power in H.p or KW, Frequency in Hz, Voltage in volts, Speed in rpm, Efficiency, Power factor, Full load Current, Type: Squirrel cage rotor or wound rotor [7, 8].

Design Equations
The design was derived as follows:

Output Equation
We have to relate the output of the machine with its main dimensions. Let us use the following nomenclature:

\[ E_{ph} = \text{Induced emf per phase in volts.}(\text{induced emf/phase = applied voltage/phase}) \]

\[ I_{ph} = \text{Current per phase, A.} \]

\[ T_{ph} = \text{No. Of turns per phase.} \]

\[ \phi = \text{Flux per pole in the air gap.} \]

\[ P = \text{No. Of poles.} \]

\[ K_w = \text{Winding Factor} \]

\[ B_{av} = \text{Average value of flux density in the airgap} \]

\[ ac = \text{Ampere conductor per meter of the armature periphery.} \]

\[ D = \text{Armature diameter or stator bore diameter.} \]

\[ L = \text{Stator core length in meter.} \]

\[ n_s = \text{Synchronous Speed in r.p.s} \]

\[ \eta = \text{Efficiency.} \]

\[ \cos \phi = \text{Full load power factor} \]

\[ \tau = \text{Pole pitch=}(\pi D)/P. \]

The KVA rating of a three phase induction motor is given by:

\[ KVA = 3 \times E_{ph} \times I_{ph} \times 10^{-3} \]

\[ KVA = 3 \times 4.44 \times K_w \times f \times \phi \times T_{ph} \times I_{ph} \times 10^{-3} \]

If the rating is given in HP or KW, we convert it to KVA by the relation:

\[ KVA = \frac{HP \times 0.746}{\eta \times \cos \phi} \]

\[ KVA = \frac{KW}{\eta \times \cos \phi} \]

Specific magnetic loading (B_{av})

\[ = \frac{\text{Total flux in the airgap}}{\text{Area of flux path in the airgap}} \]

\[ = \frac{p \phi}{\pi DL} \]

Specific electric loading (ac)

\[ = \frac{\text{Total armature ampere conductor}}{\text{Armature at the airgap}} \]

\[ = \frac{3 \times 2 \times I_{ph} \times T_{ph}}{\pi D} \]

\[ f = \frac{PN_s}{120} = \frac{Pn_s}{2} \]

From equation (4),

\[ \phi = \frac{B_{av} \times \pi DL}{P} \]

Also, from (5),

\[ T_{ph} \times I_{ph} = \frac{ac \times \pi D}{3 \times 2} \]

Substitute (7) and (8) into (1) gives:

\[ D^2 L = \frac{KVA}{C_0 n_s} \]

Where

\[ C_0 = 1.11 \times \pi^2 K_w \times B_{av} \times ac \times 10^{-3} \]

Equation (11) is the output equation of an induction motor.

Calculation of the Main Dimensions
The armature diameter D (or stator core) and stator core length L, are known as the main dimensions.

\[ D^2 L = \frac{KVA}{C_0 n_s} \text{ in m}^3 \text{ which is also the volume} \]

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\[ L = \frac{\pi D}{P} \]  

It is advisable to design the three phase induction motor for best operating power factor \([9]\). To obtain the best power factor in an induction motor the following relationship can be assumed between \( D \) and \( L \).

\[ \left( \frac{\pi D}{P} \right) \frac{L}{L} = 0.18 \left( \frac{\pi D}{P} \right) \]

Hence internal diameter of stator, \( D = 0.135P(L)^{1/2} \)  

### Periferal Velocity

The peripheral velocity \( v = \pi Dn \) m/sec  \( (15) \)

where \( n \) is in rps, \( v \) should not exceed 30m/sec for normal construction.

### Stator Calculation

#### Turns per phase

Flux per pole \( \phi = B_{00} \times \frac{\pi DL}{P} \)

Stator voltage per phase, \( E_s = 4.44K_w f_m \phi_m T_s \)  \( (16) \)

Therefore Stator winding turns per phase is:

\[ T_s = \frac{E_s}{4.44K_w f_m \phi_m} \]

where \( K_w \) is the stator winding factor.

\( T_s \) is number of stator turns.

#### Stator Conductor

\[ I_s = \frac{KVA \times 1000}{3 \times E_s} \]

Stator current per phase  \( (18) \)

Therefore,cross-sectional area of each conductor is

\[ a_s = \frac{I_s}{\delta_s} \]

Where \( \delta_s \) = Current density of stator conductor usually assumed between 3-5 A/mm\(^2\).

### Stator Slot

\( S_s = \) number of stator slot.

For a double lap winding,

\[ S_s = 2MP \]

Where \( M \) = The number of phases

\[ g = \text{number of slots per pole per phases.} \]

\( P \) = the number of poles.

\[ Y_{ss} = \frac{\pi D}{S_s} \]

The Slot pitch;  \( (21) \)

Where \( Y_{ss} \) is between 15-25mm

Total number of stator winding conductors = \( 3 \times 2 \times T_s \)  \( (22) \)

Number of conductors per slot

\[ Z_{ss} = \frac{3 \times 2 \times T_s}{S_s} \]

### Area of Conductor

Approximate area per slot = Copper section per slot/Space factor

\[ = \frac{Z_s a_s}{\text{Space factor}} \]

\[ a_s = \frac{I_s}{\delta_s} \]

Where

Where space factor varies from 0.25 to 0.4.

### AIRGAP LENGTH

\[ L_g = 0.2 + 2(DL)^{1/2} \]

where \( L_g \) is in mm

### Rotor Design

#### Rotor Slots

The first and most important thing to do here is to select the number of rotor slots in relation to the number of stator slots already selected.

\[ Y_{r} = \frac{\pi D}{S_2} \]

Rotor slot pitch =  \( (31) \)

Where \( S_2 \) is the number of rotor slots.

The number of rotor slot per pole is expressed as :

\[ S_2 = \frac{S_2}{2P} \]

\( (32) \)

#### Rotor Bar Current

If rotor mmf = 0.85 stator mmf,

Number of rotor bars \( (N_b) = \) Number of rotor slots \( S \) \( (33) \), then:

\[ I_b \times \frac{S}{r} = \]

Rotor mmf

Stator mmf

\[ = 3 \times I_s \times T_s \]  \( (20) \)
Therefore, 
\[ I_b \times S_r / 2 = 0.85(3 \times T_s \times I_s) \] 
or
\[ I_b = 0.85(6I_s \times T_s / S_r) \]  
(33)
where \( I_b \) is the rotor bar current.

Rotor Bar Area
The rotor bar area is given by:
\[ A_b = I_b / \delta_b \]  
(34)
Where: \( \delta_b \) = Current density, its value ranges between 4 to 7A/mm²

Copper Losses in the Rotor Bars
To do this, we calculate
Length of rotor bar \( l_b = L + \) Allowance for skewing.
Allowance for skewing = 5 to 8cm
Therefore, Resistance per bar, \( r_b = (0.021 + l_b) \) m² /A:mm²
Hence, total copper losses in the rotor bars
\[ = (l_b)^2 \times r_b \times \text{number of rotor bar} \]  
(35)

End Ring Current
\[ I_{e(max)} = \frac{1}{2} \left( \frac{\text{Number of rotor bars}}{\text{Number of poles}} \right) I_{b(av)} \]
But for sine wave, \( I_{b(av)} = I_b / 1.11. \) (1.11 is form factor for sine wave)
\[ I_e = \frac{S_r I_b / \pi P}{\delta_e} \]  
(37)

Area of End Rings
This is given by
\[ A_e = \frac{I_e}{\delta_e} \text{ mm}^2 \]  
(38)
Where end rings current density \( \delta_e \) is between 5 to 8 A/mm²

Copper Losses in End Rings
Mean length of the current path \( l_{me} = \pi D_{me} \)
Where \( D_{me} \) =mean diameter of end ring between 4 – 6 cm less than rotor diameter.
Resistance of end Ring
\[ r_e = \frac{0.021 \times I_{me}}{A_e} \]
where \( I_{me} \) is in m and \( A_e \) in mm².
Therefore, Total copper losses in the end rings is
\[ L_e = 2 \times I_e^2 \times r_e \]  
(39)

RESULTS
Previously, some parameters were derived equations 1-39, which aid in the design of three phase induction motor. This involves carrying out an analytical calculation or test using some given specifications. The specifications are presented as follows:

The Specifications
Rated Output = 10HP.
Voltage \( V = 415V. \)
Supply Frequency \( f = 50Hz. \)
Number of Phases \( m = 3. \)
Type of connection \( \Delta = \text{Delta}. \)
Number of poles \( P = 4. \)
Full load Efficiency \( \eta = 0.87. \)
Full load power factor = 0.87.
Specific magnetic loading \( B_{av} = 0.45\text{wb/m}^2. \)
Specific electric loading \( a_c = 23,000 \text{ A/m.} \)
Gross core length \( L = 140\text{mm.} \)
Pole pitch \( \tau_p = 129.59\text{mm.} \)
Winding type = Single layer mush.
Stator Winding factor \( K_{ws} = 0.955. \)
Number of stator slot \( S_s = 36. \)
Stator current density \( \delta_s = 3.93 \text{ A/mm}^2. \)
Stator slot per pole per phase \( g = 3. \)
Rotor diameter \( D_r = 164.3\text{mm.} \)
Number of rotor slots \( S_r = 44 \)
Type of rotor winding = Cage.
Number of rotor bars per slot \( Z_{sr} = 1. \)
Rotor winding factor \( K_{wr} = 1. \)
Current density of rotor \( \delta_b = 4.99\text{A/mm}^2. \)
Length of each bar \( L_b = 180\text{mm.} \)
Depth of end ring \( d_e = 12.5\text{mm.} \)
Thickness of end ring \( t_e = 10.26\text{mm.} \)

Analytical Method
The results of the analytical method using the given specifications are as shown in Table 1.

CAD Method
This method which involves the use of computer in design processes, provides a GUI platform in which the
design specifications can be provided to generate the desired output. Using the same specifications as in the analytical method, the obtained CAD output values are shown in Table 1. Figure 1 shows the graphical user interface (GUI) of the CAD method.

Figure 1: This figure shows the GUI platform for CAD computation.

**DISCUSSION**

The computer aided design of three phase induction motor slightly varies in the values obtained for some parameters when compared to the analytical calculations. This is because these parameters are either assumed or chosen from a table of approximate values or calculated. The variance may occur due to the fact that the analytical calculations are full of approximations, time consuming, laborious and hence very prone to errors when compared to the computer aided design method. These slight differences are however negligible and most times they do not have significant effect on the design.

The CAD method when compared with the analytical method offers many advantages. As can be seen in Table 1, there is a slight variation in the result by the two approaches which even made the CAD method superior to the analytical method. These advantages include:

i. The CAD method is easy and avoids all sources of computational errors.

ii. The machine designed using the CAD method will definitely be more efficient than the one designed using analytical method. This can be seen in the losses and resistances offered by both machine conductors.
iii. The time spent in computation is much less than the time spent using analytical method.

CONCLUSION

It is concluded that in this research work it is seen from the analytical calculations carried out and the computer aided design method used that there are a slight differences in the results obtained when compared. It can be concluded that both methods gave almost the same result; but, the analytical method past through some long and tedious process of arriving at the final design parameters which were error prone hence resulted in slight differences. The slight differences in the output result are very negligible. Finally, the product final performance is better in the computer aided design than the analytical method and the computer aided design is less time consuming and highly recommended.

Table 1: This table shows both analytical results and CAD results

<table>
<thead>
<tr>
<th>Induction Motor Parameter</th>
<th>Analytical results</th>
<th>Computer aided design results</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Output</td>
<td>Output</td>
</tr>
<tr>
<td>The revolution per minute</td>
<td>1500</td>
<td>1500</td>
</tr>
<tr>
<td>The revolution per seconds</td>
<td>25</td>
<td>25</td>
</tr>
<tr>
<td>The power in KVA is</td>
<td>9.86</td>
<td>9.86</td>
</tr>
<tr>
<td>The Coefficient Co is</td>
<td>108.31</td>
<td>108.31</td>
</tr>
<tr>
<td>The value of D*L is</td>
<td>0.0036414m³</td>
<td>0.003640m³</td>
</tr>
<tr>
<td>The value of D is</td>
<td>0.1625m</td>
<td>0.1625m</td>
</tr>
<tr>
<td>The value of L is</td>
<td>0.1379m</td>
<td>0.1379m</td>
</tr>
<tr>
<td>The flux per pole is</td>
<td>7.9209mwb</td>
<td>7.918mwb</td>
</tr>
<tr>
<td>Turns per phase</td>
<td>247.125</td>
<td>247.22</td>
</tr>
<tr>
<td>Stator current</td>
<td>7.92A</td>
<td>7.916A</td>
</tr>
<tr>
<td>Area of each conductor</td>
<td>2.01mm²</td>
<td>2.01mm²</td>
</tr>
<tr>
<td>Stator slots</td>
<td>36</td>
<td>36</td>
</tr>
<tr>
<td>Conductors per slots</td>
<td>41.19</td>
<td>41.2</td>
</tr>
<tr>
<td>Area per slot</td>
<td>86.91</td>
<td></td>
</tr>
<tr>
<td>Air gap length</td>
<td>0.3497m</td>
<td>0.3497m</td>
</tr>
<tr>
<td>Slot pitch</td>
<td>0.014180m</td>
<td>0.014182m</td>
</tr>
<tr>
<td>Stator Resistance</td>
<td>2.11ohms</td>
<td>2.108ohms</td>
</tr>
<tr>
<td>Stator copper loss</td>
<td>397.06w</td>
<td>396.375w</td>
</tr>
<tr>
<td>Rotor</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rotor Slot pitch</td>
<td>11.730mm</td>
<td>11.733mm</td>
</tr>
<tr>
<td>Rotor bar current</td>
<td>226.86A</td>
<td>226.85A</td>
</tr>
<tr>
<td>Rotor bar area</td>
<td>45.46mm²</td>
<td>45.46mm²</td>
</tr>
<tr>
<td>End ring current</td>
<td>794.36A</td>
<td>794.19A</td>
</tr>
<tr>
<td>End ring area</td>
<td>128.25mm²</td>
<td>128.25mm²</td>
</tr>
<tr>
<td>Resistance per bar</td>
<td>0.00008315ohms</td>
<td>0.00008300ohms</td>
</tr>
<tr>
<td>Resistance in the end ring</td>
<td>0.00006431ohms</td>
<td>0.00006400ohms</td>
</tr>
<tr>
<td>End ring losses</td>
<td>81.60w</td>
<td>81.13w</td>
</tr>
<tr>
<td>Copper losses in the rotor bar</td>
<td>188.31w</td>
<td>188.27w</td>
</tr>
<tr>
<td>Total losses in the rotor bar</td>
<td>269.47w</td>
<td>269.40w</td>
</tr>
</tbody>
</table>

REFERENCES


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Nil

CONFLICT OF INTEREST
No conflicts of interests were declared by authors.

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